### 9.4 Volumes of Prisms

## Essential Question

How can you find the volume of a prism?

## 1 ACTIVIJY: Pearls in a Ireasure Chest

Work with a partner. A treasure chest is filled with valuable pearls. Each pearl is about 1 centimeter in diameter and is worth about $\$ 80$.
Use the diagrams below to describe two ways that you can estimate the number of pearls in the treasure chest.

b.

c. Use the method in part (a) to estimate the value of the pearls in the chest.

## Geometry

In this lesson, you will

- find volumes of prisms.
- solve real-life problems.

Learning Standard 7.G. 6

## 2 ACJIVIJY: Finding a Formula for Volume

Work with a partner. You know that the formula for the volume of a rectangular prism is $V=\ell w h$.
a. Write a formula that gives the volume in terms of the area of the base $B$ and the height $h$.
b. Use both formulas to find the volume of each prism. Do both formulas give you the same volume?


## 3 ACTIVIJY: Finding a Formula for Volume

## Math Practice

Use a Formula
What are the given quantities? How can you use the quantities to write a formula?

Work with a partner. Use the concept in Activity 2 to find a formula that gives the volume of any prism.


## 4 ACTIVIJY: Using a Formula

Work with a partner. A ream of paper has $\mathbf{5 0 0}$ sheets.
a. Does a single sheet of paper have a volume? Why or why not?
b. If so, explain how you can find the volume of a single sheet of paper.


## What is Your Answer?

5. IN YOUR OWN WORDS How can you find the volume of a prism?
6. STRUCTURE Draw a prism that has a trapezoid as its base. Use your formula to find the volume of the prism.

## Practice

The volume of a three-dimensional figure is a measure of the amount of space that it occupies. Volume is measured in cubic units.

## Key Idea

## Volume of a Prism

Words The volume $V$ of a prism is the product of the area of the base and the height of the prism.


Algebra


## EXAMPLE (1) Finding the Volume of a Prism

## Study Tip

The area of the base of a rectangular prism is the product of the length $\ell$ and the width $w$.
You can use $V=\ell w h$ to find the volume of a rectangular prism.

Find the volume of the prism.

$$
\begin{aligned}
V & =B h & & \text { Write formula for volume. } \\
& =6(8) \cdot 15 & & \text { Substitute. } \\
& =48 \cdot 15 & & \text { Simplify. } \\
& =720 & & \text { Multiply. }
\end{aligned}
$$

$\because$ The volume is 720 cubic yards.


## EXAMPLE 2 Finding the Volume of a Prism

Find the volume of the prism.

$$
\begin{aligned}
V & =B h & & \text { Write formula for volume. } \\
& =\frac{1}{2}(5.5)(2) \cdot 4 & & \text { Substitute. } \\
& =5.5 \cdot 4 & & \text { Simplify. } \\
& =22 & & \text { Multiply. }
\end{aligned}
$$

$\therefore$ The volume is 22 cubic inches.

## On Your Own

Now You're Ready Exercises 4-12

Find the volume of the prism.
1.

2.


## EXAMPLE

## (3) Real-Life Application

A movie theater designs two bags to hold 96 cubic inches of popcorn. (a) Find the height of each bag. (b) Which bag should the theater

Bag A
 choose to reduce the amount of paper needed? Explain.
a. Find the height of each bag.

Bag B


Bag A

## Bag B

$\because$ The height is 8 inches. $\because$ The height is 6 inches.
b. To determine the amount of paper needed, find the surface area of each bag. Do not include the top base.

$$
\begin{aligned}
& \quad \text { Bag A } \\
& S=\ell w+2 \ell h+2 w h \\
&=4(3)+2(4)(8)+2(3)(8) \\
&=12+64+48 \\
&=124 \mathrm{in} .^{2}
\end{aligned}
$$

$$
\begin{aligned}
V & =B h \\
96 & =4(4)(h) \\
96 & =16 h \\
6 & =h
\end{aligned}
$$

$\therefore$ The surface area of Bag B is less than the surface area of Bag A. So, the theater should choose Bag B.

## On Your Own

3. You design Bag $C$ that has a volume of 96 cubic inches. Should the theater in Example 3 choose your bag? Explain.


## Vocabulary and Concept Check

1. VOCABULARY What types of units are used to describe volume?
2. VOCABULARY Explain how to find the volume of a prism.
3. CRITICAL THINKING How are volume and surface area different?

## Practice and Problem Solving

Find the volume of the prism.
(1) (2)
4.

5.

6.

7.

8.

9.

10.

11.

12.

13. ERROR ANALYSIS Describe and correct the error in finding the volume of the triangular prism.

14. LOCKER Each locker is shaped like a rectangular prism. Which has more storage space? Explain.
15. CEREAL BOX A cereal box is 9 inches by 2.5 inches by 10 inches. What is the volume of the box?

## Find the volume of the prism.


18. LOGIC Two prisms have the same volume. Do they always, sometimes, or never have the same surface area? Explain.
19. CUBIC UNITS How many cubic inches are in a cubic foot? Use a sketch to explain your reasoning.
20. CAPACITY As a gift, you fill the calendar with packets of chocolate candy. Each packet has a volume of 2 cubic inches. Find the maximum number of packets you can fit inside the calendar.
21. PRECISION Two liters of water are poured into an empty vase shaped like an octagonal prism. The base area is 100 square centimeters. What is the height of the water? $\left(1 \mathrm{~L}=1000 \mathrm{~cm}^{3}\right)$

22. GAS TANK The gas tank is $20 \%$ full. Use the current price of regular gasoline in your community to find the cost to fill the tank. $\left(1 \mathrm{gal}=231 \mathrm{in} .{ }^{3}\right)$
23. OPEN-ENDED You visit an aquarium. One of the tanks at the aquarium holds 450 gallons of water. Draw a diagram to show one possible set of dimensions of the tank.
$\left(1 \mathrm{gal}=231 \mathrm{in} .^{3}\right)$
24. Thinking How many times greater is the volume of a triangular prism when one of its dimensions is doubled? when all three dimensions are doubled?

(A) Fair Game Review what you learned in previous grades \& lessons

Find the selling price. (Section 6.6)
25. Cost to store: $\$ 75$

Markup: 20\%
26. Cost to store: $\$ 90$

Markup: 60\%
27. Cost to store: $\$ 130$

Markup: 85\%
28. MULTIPLE CHOICE What is the approximate surface area of a cylinder with a radius of 3 inches and a height of 10 inches? (Section 9.3)
(A) $30 \mathrm{in}^{2}$
(B) $87 \mathrm{in}^{2}$
(C) $217 \mathrm{in} .^{2}$
(D) $245 \mathrm{in}^{2}$

